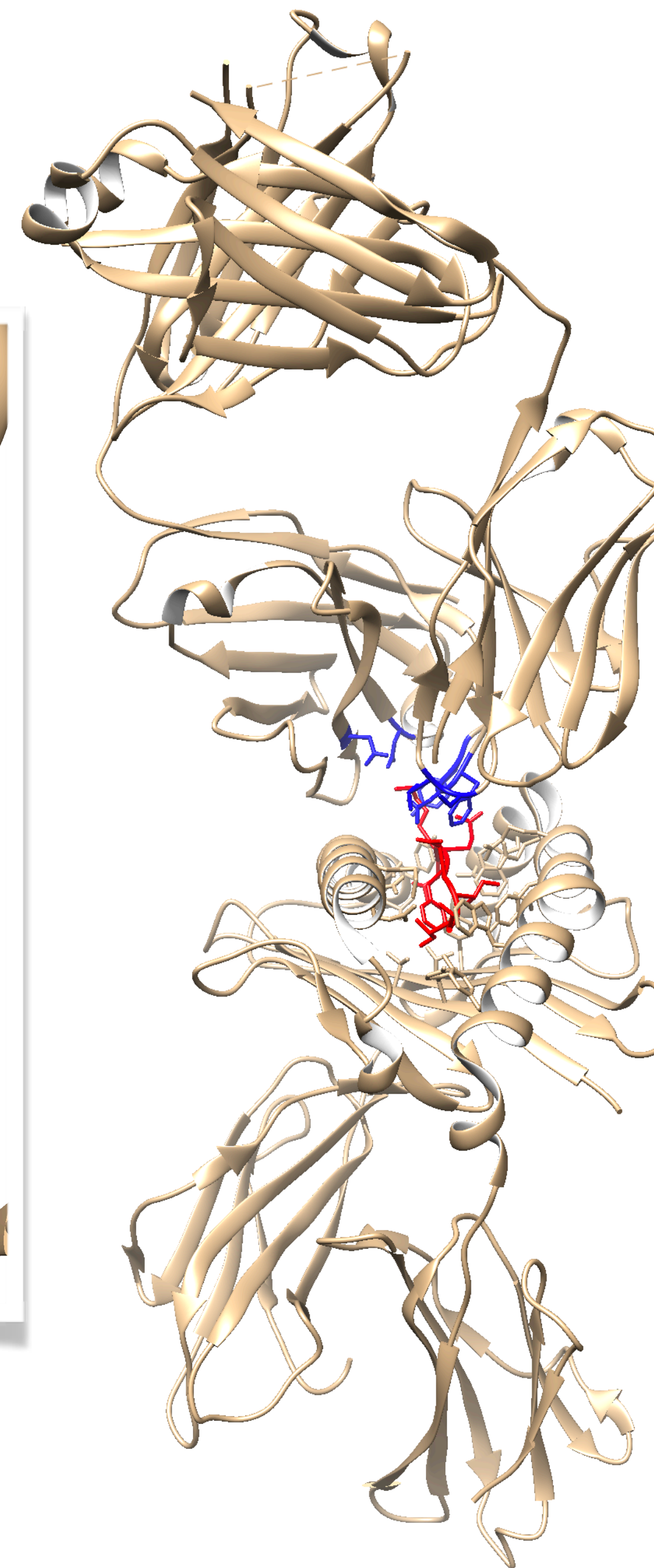
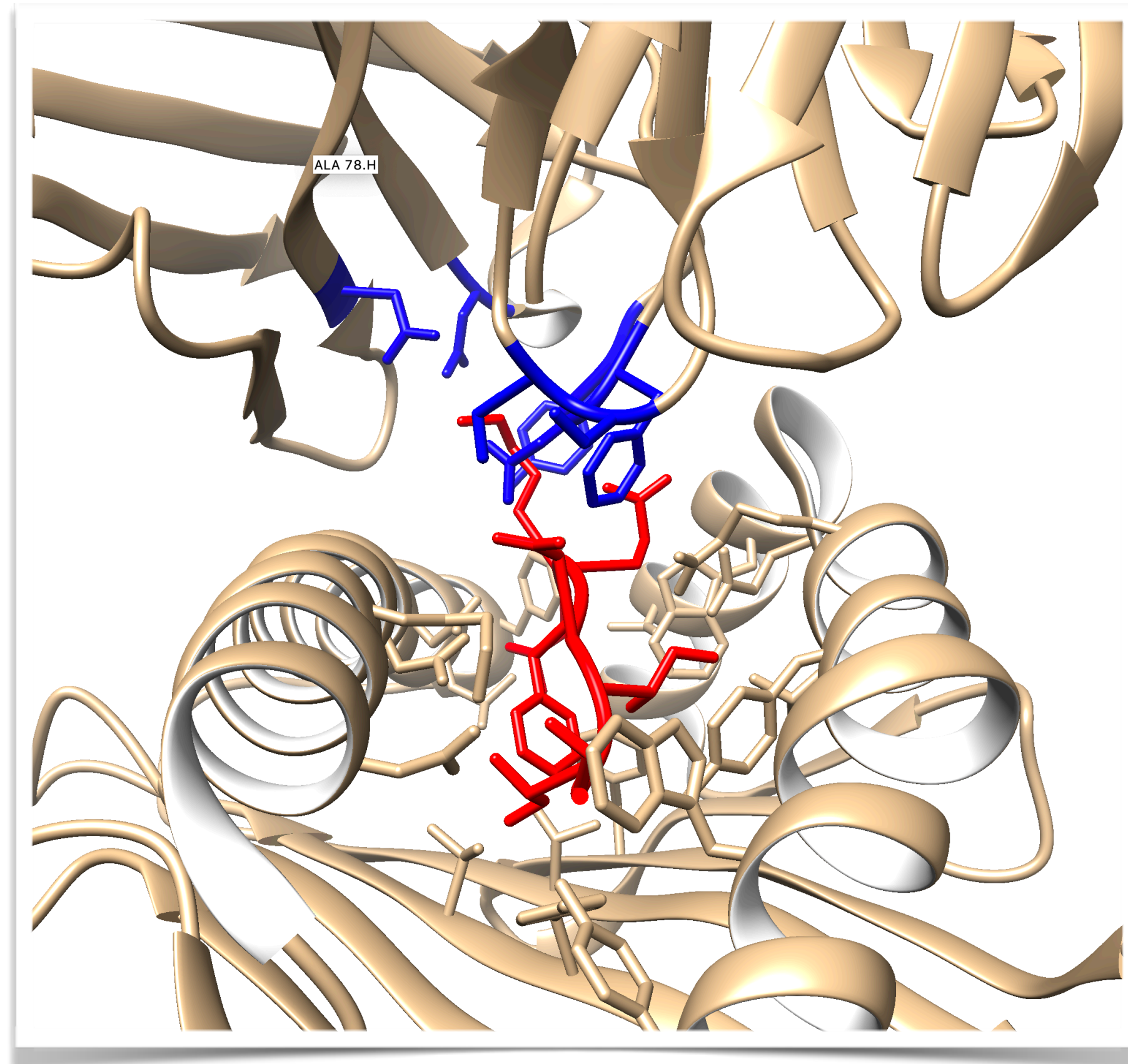


LECTURE 5

MODELING REACTIONS



Idealized model
Molecular collisions
Maxwell-Boltzman distribution (1860)
Positions (dv/V)
Velocities $(\sim m/T)^{1.5} \exp(-mv^2/T)$
Probability formulation (collision \times energy)
Propensity function ($k \times 1 \times 2$)
Diffusion ($dc/dt = D d^2c/dx^2 c$)
Stokes-Einstein equation ($D = kBT/6\pi \eta r$)
Diffusion limited $k/(1+a/D) \times 1 \times 2$
Markov chain formulation
Chemical master equation
SSA algorithms
Mass action law
ODE model
Gene expression
Explicit solution
Rise time calculation
Degradation dependence

BIONUMBERS
(<https://bionumbers.hms.harvard.edu/>)
Transcription rate (20-40nt/sec)
mRNA export time (1-10min)
Translation rate (5-10 codons/sec)
Folding time (10-30min/protein)
Diffusion time yeast (0.5sec)
Diffusion distance \sqrt{Dt}
Diffusion rate in cytoplasm ($8\mu m^2/sec$)
Diffusion rate in water ($100\mu m^2/sec$)
ER flux yeast (460molecules/sec)
Secretion time ($\sim 20min$)

Time scale separation
Fast dynamics
Slow dynamics
Enzyme reactions
Gene regulation
Positive regulation
Negative regulation
Transcription regulatory networks

EXERCISE
Create a CRR schematic for gene expression
Formulate ODE model using mass action law
Parametrize the model
Simulate the model for different degradation rates
Compute the 50% rise time